

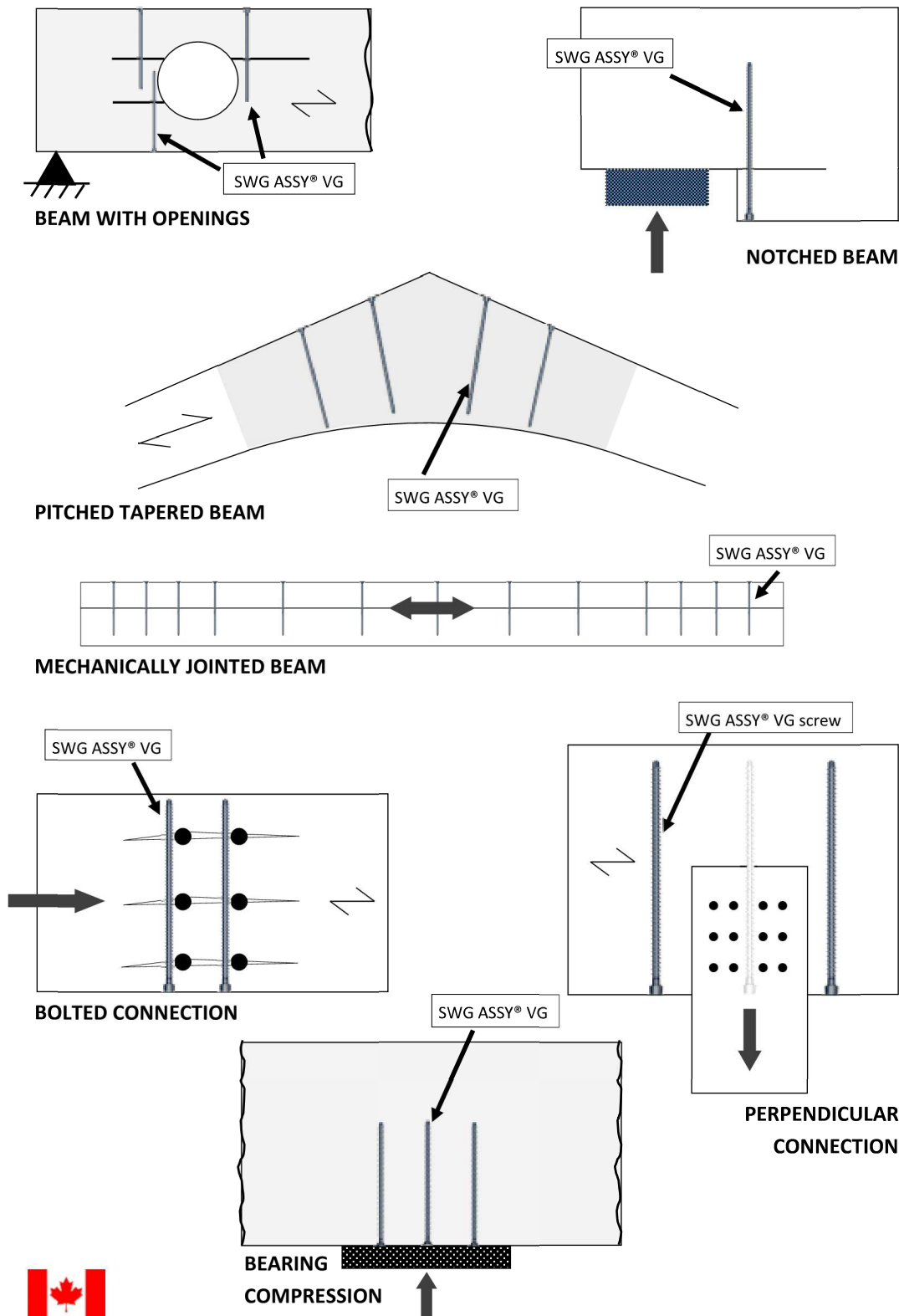
MyTiCon Timber Connectors White Paper



Full thread SWG ASSY® Screws as Reinforcement

By Max Closen Dipl.-Ing (FH), MaSc

WOOD you like to CONNECT?



CONTACT US
sales@my-ti-con.com

West Coast

604.349.8426

East Coast

438.862.1226

Technical Support

604.347.7049

info@my-ti-con.com

Conditions of use and requirements as reinforcement perpendicular to the grain

External loads on cross connections, notched beams, beams with holes, curved or pitched beams cause stress perpendicular to the grain. As perpendicular to grain splitting is among the weakest properties of wood forces in this direction typically challenge the designer.

Whenever the perpendicular to grain stress exceeds the resistance reinforcement is required.

This document provides design proposals and examples on designing perpendicular to grain reinforcements with full thread screws and does not cover any other potentially required designs of a structural member.

For tensile reinforcement perpendicular to the grain only SWG ASSY® VG screws with full thread shall be used. The screws are driven into the member perpendicular to the contact surface at an angle between screw axis and wood grain of 90°.

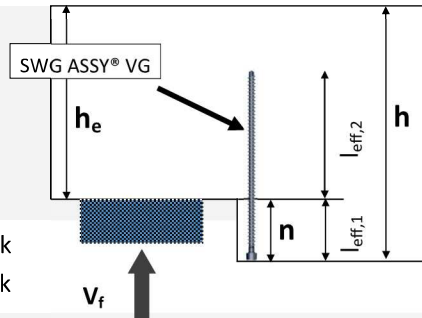
The provided design proposals are only applicable to the following timber species:

- Solid timber [softwood or hardwood (species beech or oak)]
- Glue-laminated timber
- Glued solid timber made of softwood or special hardwood (species beech or oak)
- Laminated Veneer Lumber (LVL)

Notched beam reinforcement

Notched beams experience stress concentrations which may exceed specified capacities of the beam. In these areas a combination of stresses may require beam reinforcement.

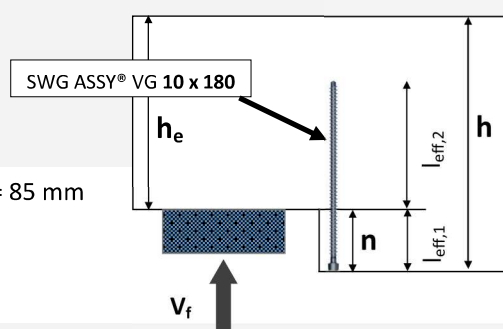
Reinforcement can be applied using self-tapping full thread SWG ASSY® VG screws. It is assumed that a check or split has already occurred in the corner of the notch and the entire transverse shear force occurring in the lower portion of the beam is to be transmitted through an axial force component in the screw. In longitudinal direction of the beam only one screw row shall be taken into account.

DESIGN NOTCHED BEAM REINFORCEMENT	
Conditions of use	rectangular glue-laminated timber member with notch at the tension side at supports
Geometry	<div> <div> b = beam width h = beam depth n = notch depth h_e = distance from potential crack to the edge </div>  </div>
Effective thread length	$l_{eff,1}$ = threaded length below potential crack $l_{eff,2}$ = threaded length above potential crack
Longitudinal shear resistance [1]	$F_v = f_v (K_D K_H K_{Sv} K_T) \text{ [N/mm}^2\text{]}$
Maximum shear resistance [1]	$V_{r,max}$
Existing bearing reaction shear force	V_f
CONDITION	IF $V_f \geq V_{r,max}$ REINFORCEMENT IS REQUIRED
Factors [2] (k_α values for standard α ratios are calculated in table 2)	$\alpha = (h_e/h)$ $k_\alpha = 1.3 * [3 * (1-\alpha)^2 - 2 * (1-\alpha)^3]$
Tensile design force [2] to be transmitted by the reinforcing SWG ASSY® VG screws	$V_{r,t,90} = k_\alpha * V_f$
boundary conditions for screw design withdrawal resistance [12]	<u>effective screw length:</u> $l_{eff} = \min \{l_{eff,1}; l_{eff,2}\}$ <u>minimum penetration depth:</u> $p_{min} = 4 * D$ (outside thread diameter) $\leq l_{eff}$ (smaller penetration can not be taken into account for beam reinforcement)
Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} \text{withdrawal resistance [kN/20 mm]} * l_{eff} \\ \text{tensile resistance} \end{array} \right.$
Required number of reinforcing screws ¹	$n_{screws} = 0.9 \sqrt{V_{r,t,90} / P'_{rw,\alpha}}$

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

A minimum of 2 screws shall be used whereas only one may be used when minimum penetration depth below and above potential crack is $20 * D$ (=outer thread screw diameter). Required spacing, end and edge distances as per table 6 to be followed

EXAMPLE NOTCHED BEAM REINFORCEMENT

Example	GL 24f-E 215 x 456 mm (8.5 x 18"), $K_D = K_H = K_{Sf} = K_T = 1$, single span over 6 m (19.7')
Geometry	$b = 215 \text{ mm (8.5")}$ $h = 456 \text{ mm (18")}$ $n = 100 \text{ mm (4")}$ $h_e = 456 - 100 = 356 \text{ mm}$ 
Effective thread length	$l_{eff,1} = 100 - 15 \text{ (unthreaded head)} = 85 \text{ mm}$ $l_{eff,2} = l_{screw} - n - l_{tip} (=D) = 180 - 100 - 10 = 70$
Longitudinal shear resistance	$F_v = 2 * 1 = 2 \text{ N/mm}^2$
Maximum shear resistance [1]	$K_N = (1 - 100/456)^2 = 0.61$ $A_g = 215 * 456 = 98,040 \text{ mm}^2$ $V_{r,max} = 0.9 * 2 * 2/3 * 98,040 * 0.61 = 71.7 \text{ kN}$
Existing bearing reaction shear force	$V_f = 100 \text{ kN}$
CONDITION	100 > 71.7 → REINFORCEMENT IS REQUIRED
Factors [2] (k_α values for standard α ratios are calculated in table 2)	$\alpha = (356/456) = 0.78$ $k_\alpha = 0.161 \text{ (table 2)}$
Tensile design force [2] to be transmitted by the reinforcing SWG ASSY® VG screws	$V_{r,t,90} = 0.161 * 100 = 16.1 \text{ kN}$
boundary conditions for screw design withdrawal resistance [12]	effective screw length: $l_{eff} = \min \{70 ; 85\} = 70 \text{ mm}$ minimum penetration depth : $p_{min} = 4 * 10 = 40 < 70 \quad \checkmark$
Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} 2.00 \text{ kN/20 mm} * 70 \text{ mm} = \underline{7 \text{ kN}} \\ 19.2 \text{ kN} \end{array} \right.$
Required number of reinforcing screws ¹	$n_{screws} = 0.9 \sqrt{(16.1 / 7)} = 2.5 \rightarrow \text{3 screws of type SWG ASSY® VG CYL 10 x 180}$

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

A minimum of 2 screws shall be used whereas only one may be used when minimum penetration depth below and above potential crack is 20*D (=outer thread screw diameter). Required spacing, end and edge distances as per table 6 to be followed

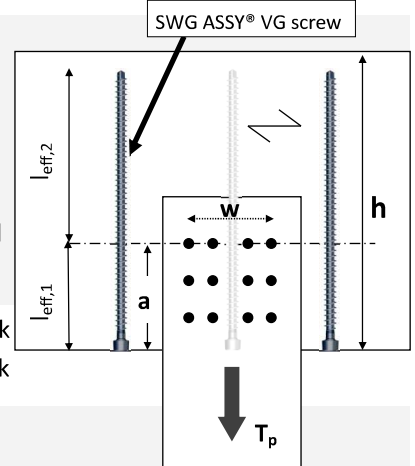
Perpendicular connection members with reinforcement

Perpendicular to grain reinforcement may be required to reduce the potential of perpendicular to grain splitting. The zone at risk is in the outer row of fasteners to the edge of the beam.

Reinforcement can be applied using self-tapping full thread SWG ASSY® VG screws.

Outside of the connection only one screw row in longitudinal direction of the beam shall be taken into account.

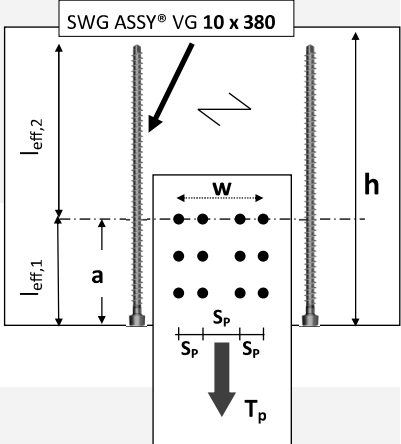
DESIGN PERPENDICULAR CONNECTION WITH REINFORCEMENT

Conditions of use	Perpendicular to grain loaded beam
Geometry	<p> b = beam width [mm] h = beam depth [mm] a = distance measured from the center of the upper row of fasteners (potential crack) to the loaded edge w = width of connection less the included fastener diameters </p> 
Effective thread length	<p> $l_{eff,1}$ = threaded length below potential crack $l_{eff,2}$ = threaded length above potential crack </p>
Tensile strength perpendicular to grain [1]	$F_{tp} = f_{tp} (K_D K_H K_{Sf} K_T) \text{ [N/mm}^2\text{]}$
Net tension resistance	$T_{r,tp,max} = \phi (=0.7) * F_{tp} * A_n$ with $A_n = b * w \text{ [mm}^2\text{]}$
Existing vertical connection shear force	T_p
CONDITION	IF $T_p \geq T_{r,tp,max}$ REINFORCEMENT IS REQUIRED
factors [3] (k_{tp} values for standard α ratios are calculated in table 3)	$\alpha = (a/h)$
	$k_{tp} = [1 - 3 * \alpha^2 + 2 * \alpha^3]$
Tensile design force [3] to be transmitted by the reinforcing SWG ASSY® VG screws	$T_{r,tp,90} = k_{tp} * T_p$
boundary conditions for screw design withdrawal resistance [12]	<p>effective screw length: $l_{eff} = \min \{l_{eff,1}; l_{eff,2}\}$</p> <p>minimum penetration depth: $p_{min} = 4 * D$ (outside thread diameter) $\leq l_{eff}$ (smaller penetration can not be taken into account for beam reinforcement)</p>
Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} \text{withdrawal resistance [kN/20 mm]} * l_{eff} \\ \text{tensile resistance} \end{array} \right.$
Required number of reinforcing screws ¹	$n_{screws} = 0.9 \sqrt{(T_{r,tp,90} / P'_{rw,\alpha})}$

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

A minimum of 2 screws shall be used whereas only one may be used when minimum penetration depth below and above potential crack is $20 * D$ (=outer thread screw diameter). Required spacing, end and edge distances as per table 6 to be followed

EXAMPLE PERPENDICULAR CONNECTION WITH REINFORCEMENT

<i>Example</i>	GL 24f-E 130 x 456 mm (5-1/8 x 18"), $K_D = K_H = K_{SF} = K_T = 1$, spacing between bolts (10 x 130 mm) is $S_p = 152$ mm (6"),	
<i>Geometry</i>	$b = 130$ mm (5-1/8") $h = 456$ mm (18") $a = 305$ mm (12") $w = 3 * S_p - 3 * d$ (= bolt diameter)	
<i>Effective thread length</i>	$l_{eff,1} = 305 - 16$ (unthreaded head) = 289 mm $l_{eff,2} = l_{screw} - a - l_{tip} (\triangle D) =$ $= 380 - 305 - 10 = 65$ mm	
<i>Tensile strength perpendicular to grain [1]</i>	$F_{tp} = 0.83 * 1$ [N/mm ²]	
<i>Net tension resistance</i>	$T_{r,tp,max} = 0.7 * 0.83 * 55,380 = 32.1$ kN	with $A_n = 130 * 426 = 55,380$ mm ²
<i>Existing vertical connection shear force</i>	$T_p = 45$ kN	
CONDITION	$45 \geq 32.1 \rightarrow$ REINFORCEMENT IS REQUIRED	
<i>Factors [3]</i> (k_{tp} values for standard α ratios are calculated in table 3)	$\alpha = (305/456) = 0.67$ $k_{tp} = 0.255$	
<i>Tensile design force [3] to be transmitted by the reinforcing ASSY® VG screws</i>	$T_{r,tp,90} = 0.255 * 45 = 11.5$ kN	
<i>boundary conditions for screw design withdrawal resistance [12]</i>	<u>effective screw length:</u> $l_{eff} = \min \{289 ; 65\} = 65$ mm <u>minimum penetration depth:</u> $p_{min} = 4 * 10 = 40 < 65$ ✓	
<i>Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)</i>	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} 2.00 \text{ kN}/20 \text{ mm} * 65 \text{ mm} = \underline{6.5 \text{ kN}} \\ 19.2 \text{ kN} \end{array} \right.$	
<i>Required number of reinforcing screws ¹</i>	$n_{screws} = 0.9 \sqrt{(11.5 / 6.5)} = 1.9 \rightarrow$ 2 screws of type SWG ASSY® VG CYL 10 x 380	

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

A minimum of 2 screws shall be used whereas only one may be used when minimum penetration depth below and above potential crack is $20 * D$ (=outer thread screw diameter). Required spacing, end and edge distances as per table 6 to be followed

Reinforcing openings and penetrations

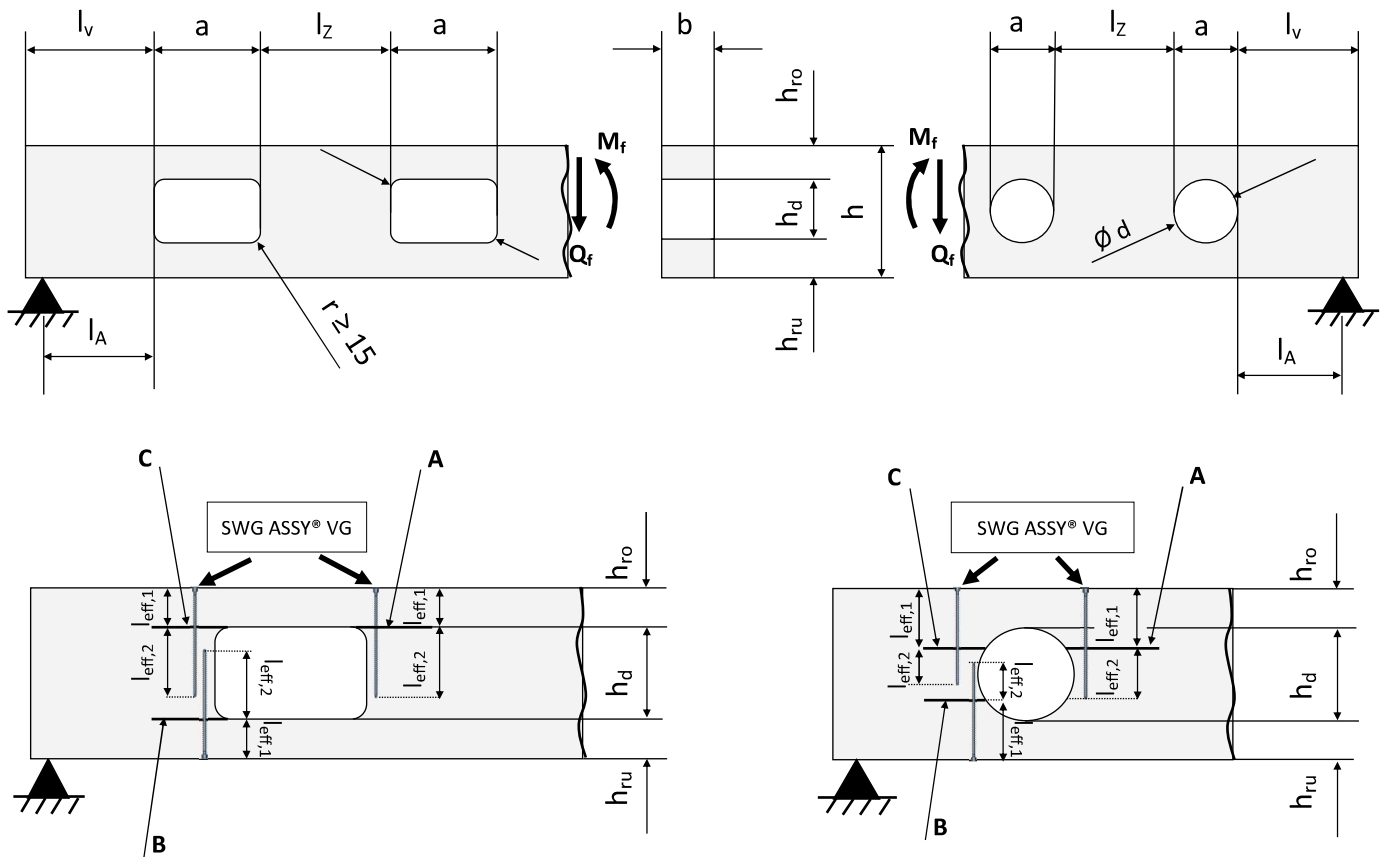
Holes greater $d = 50 \text{ mm}$ (2") may weaken the effective cross section so that shear and normal stress travel at the hole are impacted. Resulting forces perpendicular to grain may require reinforcement.

Self-tapping full thread SWG ASSY® VG screws inserted on each side of the hole are a suitable reinforcement method.

Conditions of use ¹ for reinforced beam

$l_v \geq h$	$l_z \geq \max \{h ; 300 \text{ mm}\}$	$l_A \geq h/2$	$h_{ro(ru)} \geq 0.25 * h$	$a \leq h$	$a \leq 2.5 * h_d$	$h_d \leq 0.3 * h$
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Note: ¹ according to [4]



Note:

- A potential crack on the **right side** of opening
- B potential crack on the **left side** of opening, if $F_{t,M,r} \leq F_{t,V,r}$
- C **additional** potential crack to B on the **left side** of opening, if $F_{t,M,r} > F_{t,V,r}$

right side: side of opening or penetration away from bearing area

left side: side of opening or penetration close to bearing area

DESIGN REINFORCEMENT FOR BEAMS WITH OPENINGS AND PENETRATIONS

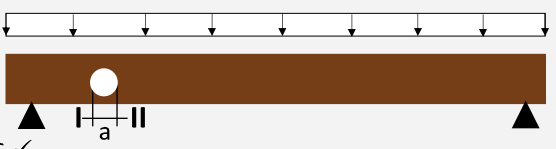
Conditions of use	beam with penetration in the high shear zone
Geometry	b = beam width h = beam depth a = length resp. diameter of the hole
Effective thread length	<u>Rectangular hole:</u> $l_{eff,1} = \min \{h_{ro}; h_{ru}\}$ less unthread head part $l_{eff,2}$ = remaining threaded length less tip length (tip length = outer thread diameter) <u>Circular hole:</u> $l_{eff,1} = \min \{h_{ro} + 0.15 * h_d; h_{ru} + 0.15 * h_d\}$ less unthread part $l_{eff,2}$ = remaining threaded length less tip length
Tensile strength perpendicular to grain [1]	$F_{tp} = f_{tp} (K_b K_H K_{Sf} K_T) \text{ [N/mm}^2\text{]}$
Design and reduction factors [5]	<u>Rectangular hole:</u> $l_{t,90} = 0.5 * (h_d + h)$ <u>Circular hole:</u> $l_{t,90} = 0.353 * h_d + 0.5 * h$ $k_{t,90} = \min \{ (450/h)^{0.5}; 1 \}$
Net tension resistance [5]	$T_{r,tp,max} = 0.5 * l_{t,90} * b * k_{t,90} * \phi (=0.7) * F_{tp}$
External load at section	Q_f, M_f
Reduced height [5]	<u>Rectangular hole:</u> $h_r = \min \{h_{ro}; h_{ru}\}$ <u>Circular hole:</u> $h_r = \min \{h_{ro} + 0.15 * h_d; h_{ru} + 0.15 * h_d\}$
Design stress [5] at opening perpendicular-to-grain from shear	$F_{t,v,r} = (Q_f * h_d) / (4 * h) * [3 - (h_d^2 / h^2)]$
Design stress [5] at opening perpendicular-to-grain from bending	$F_{t,m,r} = 0.008 * M_f / h_r$
Resulting design stress [5] at opening perpendicular-to-grain	$F_{t,r} = F_{t,v,r} + F_{t,m,r}$
CONDITION	IF $F_{t,r} \geq T_{r,tp,max}$ REINFORCEMENT IS REQUIRED
Tensile design force [5] to be transmitted by the reinforcing SWG ASSY® VG screws ¹	$F_{t,r} = F_{t,v,r} + F_{t,m,r}$
boundary conditions for screw design with-drawal resistance [12]	<u>effective screw length:</u> $l_{eff} = \min \{l_{eff,1}; l_{eff,2}\}$ <u>minimum penetration depth:</u> $p_{min} = 4 * D$ (outside thread diameter) $\leq l_{eff}$ (smaller penetration can not be taken into account for beam reinforcement)
Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} \text{withdrawal resistance [kN/20 mm]} * l_{eff} \\ \text{tensile resistance} \end{array} \right.$
Required number of reinforcing screws on one side of the hole ²	$n_{screws} = 0.9 \sqrt{(F_{t,r} / P'_{rw,\alpha})}$

Note: ¹ Additional reinforcement shall be designed if $F_{t,m,r} > F_{t,v,r}$

² considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

Screws to be driven in on each side of opening **sufficiently extending into the timber below and above opening.**

EXAMPLE REINFORCEMENT FOR BEAM WITH OPENINGS AND PENETRATIONS ¹

<i>Example</i>	Single span beam: GL 24f-E 215 x 456 mm (8.5 x 18"), $K_D = K_H = K_{Sf} = K_T = 1$, hole size: $a = 200$ in the center of the beam depth screws: SWG ASSY® VG 10 x 280
<i>Geometry</i>	$b = 215 \text{ mm (8.5")}$ $d = 456 \text{ mm (18")}$ $a = h_d = 200 \leq 456 \checkmark$ $h_{ro} = h_{ru} = (456 - 200)/2$ $= 128 \text{ mm} \geq 0.25 * 456 \checkmark$ 
<i>Effective thread length with circular hole</i>	$l_{eff,1} = 128 + 0.15 * 200 - 15 = 143$ $l_{eff,2} = 280 - 143 - 10 = 127$
<i>Tensile strength perpendicular to grain [1]</i>	$F_{tp} = 0.83 * 1 \text{ [N/mm}^2\text{]}$
<i>Design and reduction factors for circular hole</i>	$l_{t,90} = 0.353 * 200 + 0.5 * 456 = 298.6 \text{ mm}$ $k_{t,90} = \min\{ (450/456)^{0.5} ; 1 \} = 0.993$
<i>Net tension resistance [5]</i>	$T_{r,tp,max} = 0.5 * 298.6 * 215 * 0.993 * 0.7 * 0.83 = 15.9 \text{ kN}$
<i>Load at section I</i>	$Q_{f,I} = 80 \text{ kN} \quad , \quad M_{f,I} = 100 \text{ kNm}$
<i>Relative height with circular hole</i>	$h_r = 128 + 0.15 * 200 = 158 \text{ mm}$
<i>Design stress [5] at opening perpendicular-to-grain from shear</i>	$F_{t,v,r} = (80 * 200) / (4 * 456) * [3 - (200^2 / 456^2)] = 24.6 \text{ kN}$
<i>Design stress [5] at opening perpendicular-to-grain from bending</i>	$F_{t,M,r} = 0.008 * (100 * 10^3) / 158 = 5.1 \text{ kN}$
<i>Resulting design stress [5] at opening perpendicular-to-grain</i>	$F_{t,r} = 24.6 + 5.1 = 29.7 \text{ kN}$
CONDITION	$29.7 \geq 15.9 \rightarrow$ REINFORCEMENT IS REQUIRED
<i>Tensile design force [5] to be transmitted by the reinforcing ASSY® VG screws</i>	$F_{t,r} = 29.7 \text{ kN}$
<i>boundary conditions for screw design withdrawal resistance [12]</i>	<u>effective screw length:</u> $l_{eff} = \min \{ 143 ; 127 \} = 127 \text{ mm}$ <u>minimum penetration depth:</u> $p_{min} = 4 * 10 = 40 < 127 \checkmark$
<i>Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)</i>	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} 2.00 \text{ kN/20 mm} * 127 \text{ mm} = \underline{12.7 \text{ kN}} \\ 19.2 \text{ kN} \end{array} \right.$
<i>Required number of reinforcing screws ²</i>	$n_{screws} = 0.9 \sqrt{(29.7 / 12.7)} = 2.57$ \rightarrow 3 screws per side of type SWG ASSY® VG CYL 10 x 280 \rightarrow see page 6 for screw arrangement

Note: ¹ only valid if $F_{t,M,r} \leq F_{t,v,r}$

² considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

Screws to be driven in on each side of opening **sufficiently extending into the timber below and above opening**

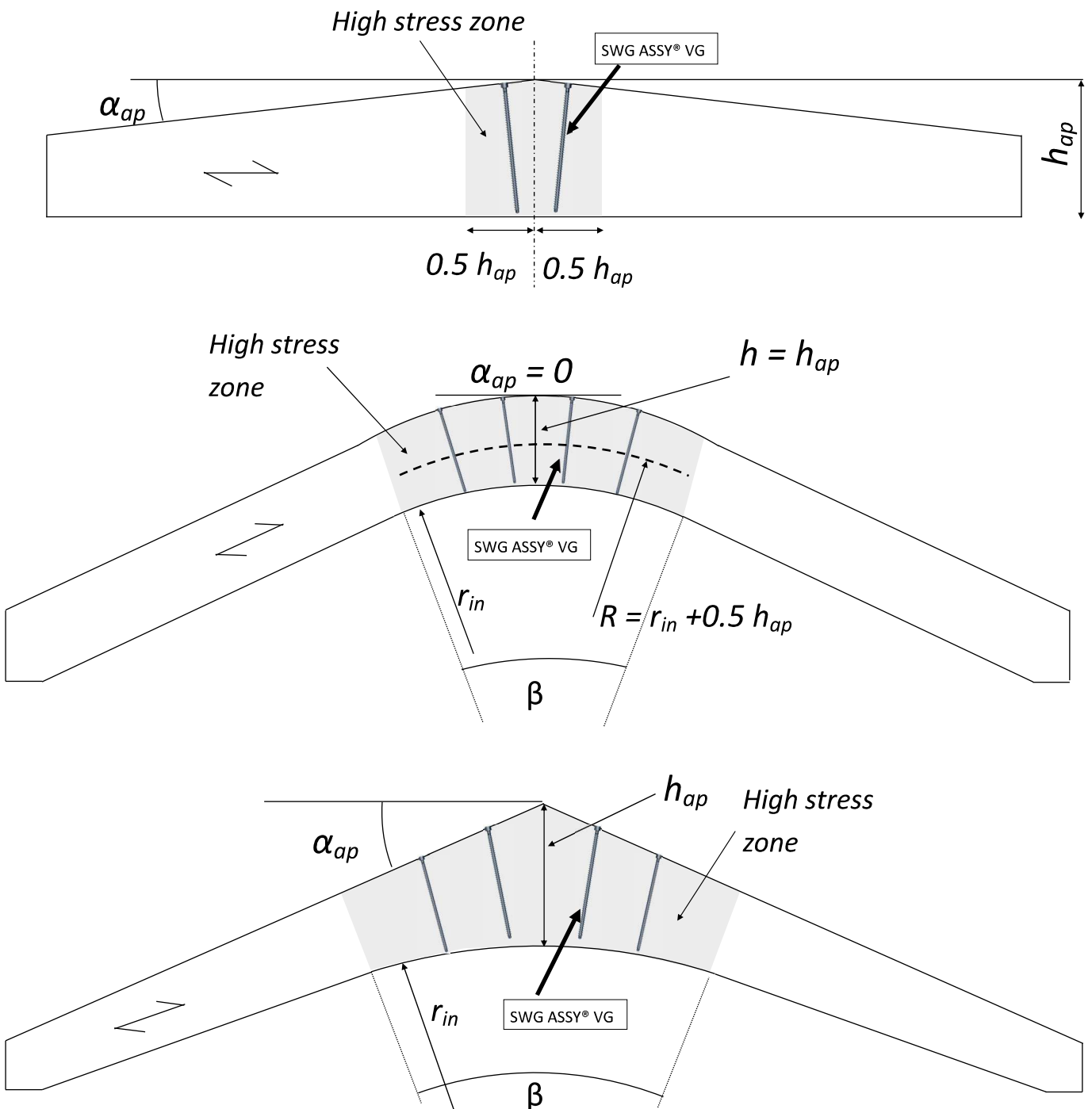
Required spacing, end and edge distances as per *table 6* to be followed.

Reinforcing pitched tapered beams

In pitched tapered beams radial tension stresses often limit the beam slope to 15° or less. Increased bending stress and tensile stress perpendicular-to-grain may occur at the apex cross section.

Reinforcement in the apex area may be applied using self-tapping full thread SWG ASSY® VG screws inserted over the beam depth in the high stressed zone.

Applicable to glue-laminated timber only.



DESIGN PITCHED TAPERED BEAM REINFORCEMENT

<i>Conditions of use</i>	Pitched tapered beam with rectangular cross section
<i>Geometry</i>	b = beam width h = beam depth h_{ap} = beam depth at the apex r_{in} = inner radius at the apex r = $r_{in} + 0.5 h_{ap}$ (radius of curvature at centreline) α_{ap} = angle of the taper in the centre of the apex β = enclosed angle in radians
<i>Effective thread length [7]</i>	Screws must penetrate the entire beam depth → $l_{screw} \approx h$ l_{eff,1} = half of the screw length less the unthreaded head part [mm] l_{eff,2} = half of the screw length less 1*D (outer thread diameter) for the tip length [mm]
<i>Tensile strength perpendicular to grain [1]</i>	F_{tp} = $f_{tp} (K_D K_H K_{Sf} K_T)$ [N/mm ²]
<i>Factored bending moment resistance [1] based on radial tension strength</i>	M_{rt}
<i>Design moment causing tensile stress</i>	M_{r,ap}
CONDITION	IF $M_{r,ap} \geq M_{rt}$ REINFORCEMENT IS REQUIRED
<i>Factors [6]</i>	k₆ = $0.25 - 1.5 \tan \alpha_{ap} + 2.6 \tan^2 \alpha_{ap}$ k₇ = $2.1 \tan \alpha_{ap} - 4 \tan^2 \alpha_{ap}$ k_p = $0.2 \tan \alpha_{ap} + k_6 (h_{ap}/r) + k_7 (h_{ap}/r)^2$
<i>Greatest tensile stress [6] perpendicular-to-grain at the apex due to bending moment</i>	σ_{r,t,90} = $k_p (6 M_{r,ap}) / (b h_{ap}^2)$ [N/mm ²]
<i>Spacing of fasteners [7]</i>	250 mm ≤ a₁ ≤ 0.75 * h_{ap}
<i>Tensile design force [7] to be transmitted by the reinforcing ASSY® VG screws</i>	F_{t,r} = $\sigma_{r,t,90} * b * a_1$
<i>boundary conditions for screw design with-drawal resistance [12]</i>	<u>effective screw length:</u> l_{eff} = $\min \{l_{eff,1}; l_{eff,2}\}$ <u>minimum penetration depth:</u> p_{min} = $4 * D$ (outside thread diameter) ≤ l _{eff} (smaller penetration can not be taken into account for beam reinforcement)
<i>Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)</i>	P'_{rw,α} = $\min \left\{ \begin{array}{l} \text{withdrawal resistance [kN/20 mm]} * l_{eff} \\ \text{tensile resistance} \end{array} \right.$
<i>Required number of reinforcing screws ¹</i>	n_{screws} = $^{0.9} \sqrt{(F_{t,r} / P'_{rw,\alpha})}$

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

A minimum of 2 reinforcing screws evenly distributed in the highly stressed apex zone shall be applied.

Required spacing, end and edge distances as per table 6 to be followed.

EXAMPLE PITCHED TAPERED BEAM REINFORCEMENT

<i>Example</i>	Pitched double-tapered beam: GL 24f-E 130 x 456 mm (5-1/8 x 18")
<i>Geometry</i>	$b = 130 \text{ mm (5-1/8")}$ $h = 456 \text{ mm (18")}$ $h_{ap} = 813 \text{ mm (32")}$ $r_{in} = 2800 \text{ mm}$ $r = 2800 + 0.5 * 813 = 3206.5 \text{ mm}$ $\alpha_{ap} = 39^\circ$ $\beta = 51.3^\circ * \pi/180^\circ$
<i>Effective thread length [7]</i>	$l_{screw} \approx h = 456 \text{ mm} \rightarrow \text{SWG ASSY}^\circ \text{ VG Cyl 10x430}$ $l_{eff,1} = 215 - 15 = 200 \text{ mm}$ $l_{eff,2} = 215 - 10 = 205 \text{ mm}$
<i>Tensile strength perpendicular to grain [1]</i>	$F_{tp} = 0.83 * 1 \text{ N/mm}^2$
<i>Factored bending moment resistance [1] based on radial tension strength</i>	$A = 130 * 813 = 105690 \text{ mm}^2 \quad K_{Ztp} = 0.7 \quad K_R = 7.0$ $M_{rt} = 0.9 * 0.83 * (130 * 813^2 / 6) * 0.7 * 7.0 = \underline{52.4 \text{ kNm}}$ $(M_{rt} = 0.9 * 0.83 * 2/3 * 105690 * 3206.5 * 0.7 = 118.1 \text{ kNm})$
<i>Design moment causing tensile stress parallel to the inner curved edge</i>	$M_{r,ap} = 70 \text{ kNm}$
CONDITION	$70 \geq 52.4 \rightarrow \text{REINFORCEMENT IS REQUIRED}$
<i>Factors [6]</i>	$k_6 = 0.25 - 1.5 * \tan 39 + 2.6 * \tan^2 39 = 0.74$ $k_7 = 2.1 * \tan 39 - 4 * \tan^2 39 = -0.92$ $k_p = 0.2 * \tan 39 + 0.74 * (813 / 3206.5) - 0.92 * (813 / 3206.5)^2 = 0.29$
<i>Greatest tensile stress [6] perpendicular-to-grain at the apex due to bending moment</i>	$\sigma_{r,t,90} = 0.29 * (6 * 70 * 10^6) / (130 * 813^2) = 1.42 \text{ N/mm}^2$
<i>Spacing of fasteners [7]</i>	$250 \text{ mm} \leq 355 (14") \leq 600$
<i>Tensile design force [7] to be transmitted by the reinforcing ASSY® VG screws</i>	$F_{t,r} = 1.42 * 130 * 355 = 65.5 \text{ kN}$
<i>boundary conditions for screw design with-drawal resistance [12]</i>	<u>effective screw length:</u> $l_{eff} = \min \{200; 205\} = 200 \text{ mm}$ <u>minimum penetration depth:</u> $p_{min} = 4 * 10 = 40 < 200 \checkmark$
<i>Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)</i>	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} 2.00 \text{ kN/20 mm} * 200 \text{ mm} = 20 \text{ kN} \\ \underline{19.2 \text{ kN}} \end{array} \right.$
<i>Required number of reinforcing screws ¹</i>	$n_{screws} = 0.9 \sqrt{65.5 / 19.2} = 3.9 \rightarrow \underline{4 \text{ SWG ASSY}^\circ \text{ VG Cyl 10x430 screws}}$

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

A minimum of 2 reinforcing screws evenly distributed in the highly stressed apex zone shall be applied.

Required spacing, end and edge distances as per table 6 to be followed.

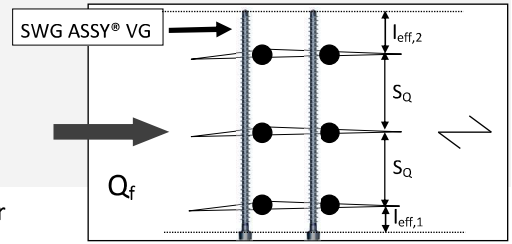
Perpendicular-to-grain splitting reinforcement in bolted connections

Bolted connections with multiple bolts per row may fail brittle due to splitting. Design codes reduce the effective number of bolts by at least 2/3 to reduce brittle failure through splitting.

Splitting perpendicular to grain can efficiently be reinforced using self-tapping full thread SWG ASSY® VG screws driven in perpendicular to the bolt axis.

The reinforcing screws with full thread shall be inserted behind the bolt (compression side) as close as possible. The reinforced connection allows to assume all bolts as active and higher connection capacities are achieved.

DESIGN REINFORCEMENT IN BOLTED CONNECTIONS

<i>Conditions of use</i>	Bolted connection loaded parallel to grain with reinforcement	
<i>Geometry</i>	b = beam width d = beam depth S_Q = spacing between bolts perpendicular to grain e_L = minimum bolt edge distance	
<i>Effective thread length</i>	l_{eff,1} = threaded length below lower potential crack l_{eff,2} = threaded length above upper potential crack less 1*D (=outer thread diameter) for the tip length	
<i>Connection parameters</i>	P_r = factored shear resistance of one bolt n_{sp} = number of shear planes per bolt	
<i>Tensile design force [8] perpendicular-to-grain to be transmitted by the reinforcing ASSY® VG screws</i>	F_{r,t,90} = n _{sp} * 0.3 * P _r	
<i>boundary conditions for screw design withdrawal resistance [12]</i>	<u>effective screw length:</u> l_{eff} = min {l _{eff,1} ; l _{eff,2} } <u>minimum penetration depth:</u> p_{min} = 4 * D (outside thread diameter) ≤ l _{eff} (smaller penetration can not be taken into account for beam reinforcement)	
<i>Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)</i>	P'_{rw,α} = min { withdrawal resistance [kN/20 mm] * l_{eff} tensile resistance	
<i>Required number of reinforcing screws ¹</i>	n_{screws} = ^{0.9} √(F _{r,t,90} / P' _{rw,α})	

Note: ¹ considering an effective number of screws n_{eff} = n^{0.9} as per [13]

Reinforcing screws **arranged adjacent to bolts**.

Required spacing, end and edge distances as per *table 6* to be followed.

EXAMPLE REINFORCEMENT IN BOLTED CONNECTIONS

Example	GL 20f-E 215 x 304 mm (8.5 x 12") connected to a beam with smallest bolt edge distance $e_L = 76 \text{ mm}$ (3") and bolt spacing perpendicular to grain $S_Q = 76 \text{ mm}$ (3") , $K_D = K_H = K_{Sf} = K_T = 1$	
Geometry	$b = 215 \text{ mm}$ (8.5") $d = 304 \text{ mm}$ (12") $S_Q = 76 \text{ mm}$ (3") $e_L = 76 \text{ mm}$ (3")	
Effective thread length	$l_{eff,1} = 76 - 15$ (unthread part) $= 61 \text{ mm}$ $l_{eff,2} = 300 - 2 * 76 - 76 - 10$ (= tip length) $= 62 \text{ mm}$	
Connection parameters	$P_r = 5.5 \text{ kN}$ $n_{sp} = 1$	
Tensile design force [8] per bolt perpendicular-to-grain to be transmitted by the reinforcing ASSY® VG screws	$F_{r,t,90} = 1 * 0.3 * 5.5 = 3.3 \text{ kN}$	
boundary conditions for screw design withdrawal resistance [12]	effective screw length: $l_{eff} = \min \{61 ; 62\} = 61 \text{ mm}$ minimum penetration depth : $p_{min} = 4 * 10 = 40 < 61 \quad \checkmark$	
Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)	$P'_{rw,\alpha} = \min \left\{ \begin{array}{l} 2.00 \text{ kN}/20 \text{ mm} * 61 \text{ mm} = \underline{\underline{6.1 \text{ kN}}} \\ 19.2 \text{ kN} \end{array} \right.$	
Required number of reinforcing screws ¹	$n_{screws} = 0.9 \sqrt{3.3 / 6.1} = 0.51 \rightarrow$ with 2 rows of fasteners 1 screw per row of type SWG ASSY® VG CYL 10 x 300 shall be used arranged adjacent to each row of bolts	

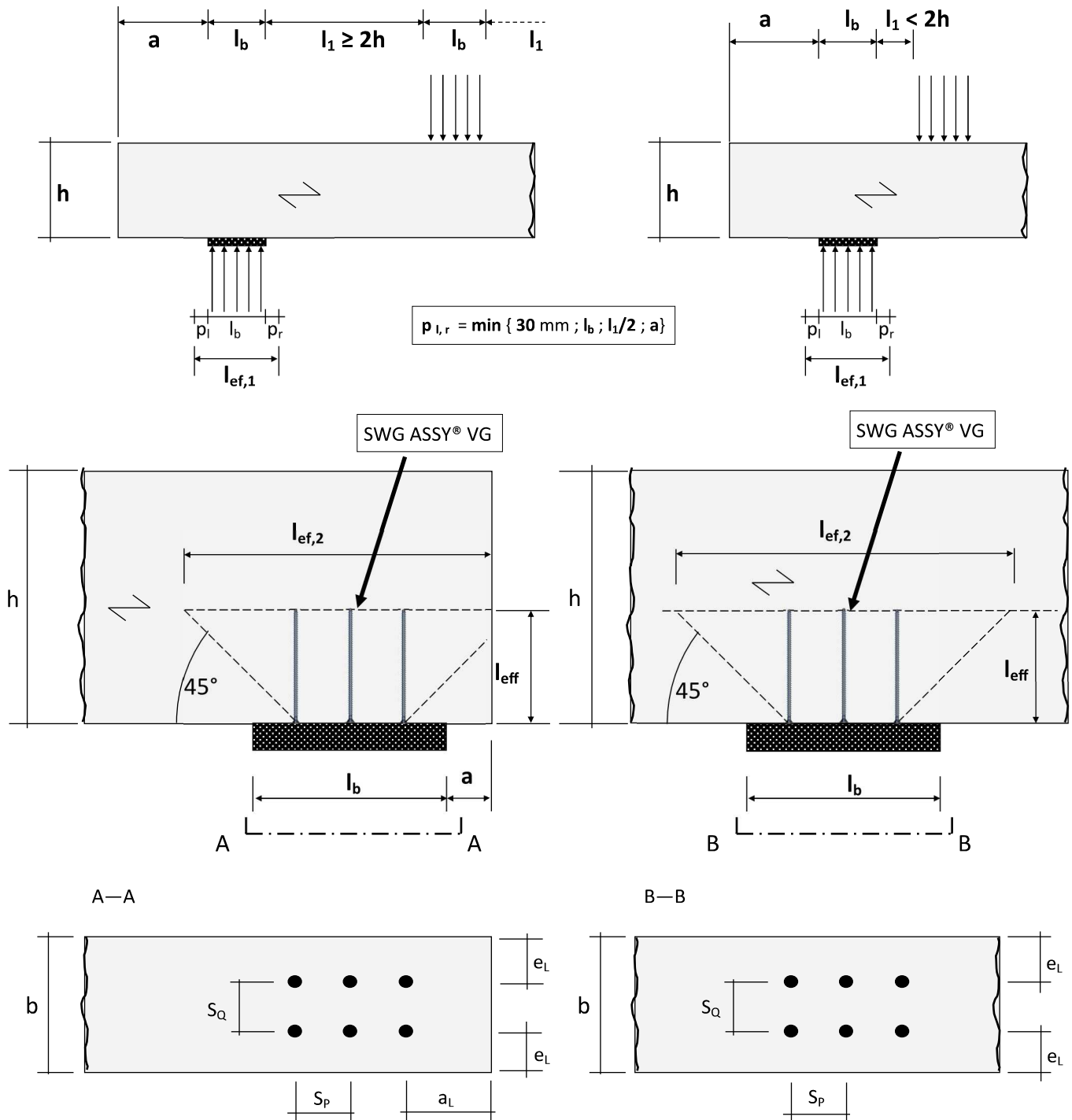
Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]

Reinforcing screws **arranged adjacent to bolts**.

Required spacing, end and edge distances as per *table 6* to be followed.

Compression reinforcement perpendicular to grain

When bearing loads exceed the compression strength of wood perpendicular to grain compression reinforcement may be applied using full thread SWG ASSY® VG screws. The screws are to be driven into the timber member perpendicular to grain top flush with the timber surface and with contact to the bearing plate to distribute the bearing force evenly.



DESIGN COMPRESSION REINFORCEMENT PERPENDICULAR TO GRAIN

Conditions of use	End or intermediate beam on discrete support								
Geometry	b = beam width h = beam depth a = distance from compressed area to beam end l_b = bearing length of support l_{eff} = threaded length less one outer thread diameter for the tip length l₁ = length between supports or incoming concentrated load n₀ = number of reinforcing screws arranged in a row parallel to grain S_p = spacing of reinforcing screws in a plane parallel to grain a_L = end distance of centre of gravity of threaded part in timber member e_L = edge distance of centre of gravity of threaded part in timber member								
Strength in compression perpendicular to grain [1]	F_{cp} = $\phi * f_{cp} * (K_D K_{Scp} K_T K_B K_{Zcp})$								
Factored compressive resistance perpendicular to grain [1]	Q_r								
Compressive design force	Q_f								
CONDITION	IF $Q_f \geq Q_r$ REINFORCEMENT IS REQUIRED								
Effective length of distribution <i>l_{ef,1}</i> [9]	<u>Effective bearing length (left, right):</u> p_{l,r} = min { 30 mm ; l _b ; l ₁ /2 ; a } l_{ef,1} = l _b + p _l + p _r								
Compressive reduction factor for discrete supports [9]	<table> <tr> <td><u>l₁ < 2h</u></td><td><u>l₁ ≥ 2h</u></td></tr> <tr> <td>k_{c,90} = 1.00</td><td>k_{c,90} = 1.75 (glulam with l_b ≤ 400 mm)</td></tr> <tr> <td></td><td>k_{c,90} = 1.50 (softwood solid sawn)</td></tr> <tr> <td></td><td>k_{c,90} = 1.00 (hardwood)</td></tr> </table>	<u>l₁ < 2h</u>	<u>l₁ ≥ 2h</u>	k _{c,90} = 1.00	k _{c,90} = 1.75 (glulam with l _b ≤ 400 mm)		k _{c,90} = 1.50 (softwood solid sawn)		k _{c,90} = 1.00 (hardwood)
<u>l₁ < 2h</u>	<u>l₁ ≥ 2h</u>								
k _{c,90} = 1.00	k _{c,90} = 1.75 (glulam with l _b ≤ 400 mm)								
	k _{c,90} = 1.50 (softwood solid sawn)								
	k _{c,90} = 1.00 (hardwood)								
Design resistance [10] perpendicular-to-grain of a contact area	R_{cb,90,d} = k _{c,90} * b * l _{ef,1} * F _{cp}								
boundary conditions for screw design compression resistance [12]	<u>Effective thread penetration length:</u> l_{eff} <u>minimum penetration depth:</u> p_{min} = 4 * D (outside thread diameter) (smaller penetration can not be taken into account for beam reinforcement)								
Compression resistance of one SWG ASSY® VG screw (refer to table 1 and 4)	withdrawal resistance [kN/20 mm] * l _{eff} (refer to table 1) P'_{rw,α} = min { tensile resistance (refer to table 1) buckling resistance of the screw (refer to table 4)								
Required number ¹ of reinforcing screws [10]	n_{screws} = $^{0.9} \sqrt{([Q_f - R_{cb,90,d}] / P'_{rw,\alpha})}$								
Effective contact length in the plane of the screw tips <i>l_{ef,2}</i> [10]	<u>End supports:</u> l_{ef,2} = { l _{eff} + (n ₀ - 1) * S _p + min (l _{eff} ; a _L) } <u>intermediate supports:</u> l_{ef,2} = { 2 * l _{eff} + (n ₀ - 1) * S _p }								
CONDITION [10]	R_{c,tip,90,d} = b * l _{ef,2} * F _{cp} ≥ Q _f → otherwise screw length or number to be adjusted								

Note: ¹ considering an effective number of screws n_{eff} = n^{0.9} as per [13]
Required spacing, end and edge distances as per table 6 to be followed

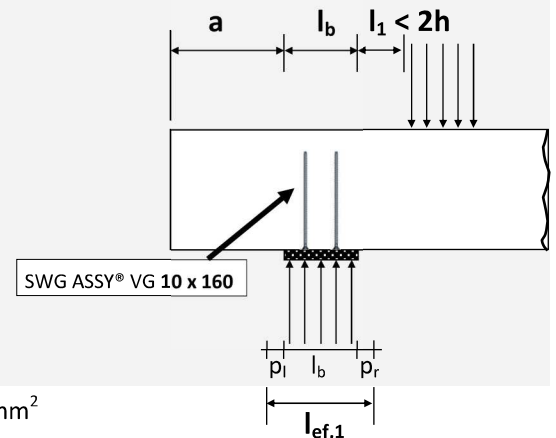
EXAMPLE COMPRESSION REINFORCEMENT PERPENDICULAR TO GRAIN

Example

GL 24f-E 215 x 456 mm (8.5 x 18") with an end support
potential reinforcement: SWG ASSY® VG CSK 10 x 160 mm

Geometry

$b = 215 \text{ mm (8.5")}$
 $h = 456 \text{ mm (18")}$
 $a = 81 \text{ mm}$
 $l_b = 100 \text{ mm}$
 $l_{eff} = 160 - 10 = 150 \text{ mm}$
 $l_1 = 750 \text{ mm}$
 $n_0 = 2$
 $S_p = 76 \text{ mm (3")}$
 $a_L = 114 \text{ mm (4-1/2")}$
 $e_L = 76 \text{ mm (3")}$



Strength in compression perpendicular to grain [1]

$$F_{cp} = 0.8 * 7 * 1.0 = 5.6 \text{ N/mm}^2$$

Factored compressive resistance perpendicular to grain [1]

$$Q_r = K_B * l_b * b * F_{cp} = 1.1 * 100 * 215 * 5.6 = 132.4 \text{ kN}$$

Compressive design force

$$Q_f = 220 \text{ kN}$$

CONDITION

220 ≥ 132.4 REINFORCEMENT IS REQUIRED

Effective length of distribution $l_{ef,1}$ [9]

Effective bearing length (left, right): $p_l = \min \{ 30 ; 100 ; 750/2 ; 81 \} = 30 \text{ mm}$
 $p_r = \min \{ 30 ; 100 ; 750/2 \} = 30 \text{ mm}$

$$l_{ef,1} = 100 + 30 + 30 = 160 \text{ mm}$$

Compressive reduction factor for discrete supports [9]

$$750 < 2 * 456 = 912 \text{ mm}$$

$$k_{c,90} = 1.00$$

Design resistance [10] perpendicular-to-grain of a contact area

$$R_{c,90,d} = 1.00 * 215 * 160 * 5.6 = 192.6 \text{ kN}$$

boundary conditions for screw design withdrawal resistance [12]

Effective thread penetration length: $l_{eff} = 150 \text{ mm}$

minimum penetration depth: $p_{min} = 4 * 10 = 40 \leq 150 \checkmark$

Compression resistance of one SWG ASSY® VG screw (refer to table 1 and 4)

$$P'_{rw,\alpha} = \min \left\{ \begin{array}{ll} 2.00 \text{ [kN/20 mm]} * 150 = \underline{15 \text{ kN}} & (\text{refer to table 1}) \\ 19.2 \text{ kN} & (\text{refer to table 1}) \\ 17.07 \text{ kN} & (\text{refer to table 4}) \end{array} \right.$$

Required number of reinforcing screws ¹

$$n_{screws} = 0.9 \sqrt{[(220 - 192.6) / 15]} = 1.95$$

→ **2 SWG ASSY® VG CSK 10 x 160 screws distributed on 2 rows**

Effective contact length in the plane of the screw tips $l_{ef,2}$ [10]

End supports: $l_{ef,2} = \{150 + (2-1) * 76 + \min (150 ; 114)\} = 340 \text{ mm}$

CONDITION [10]

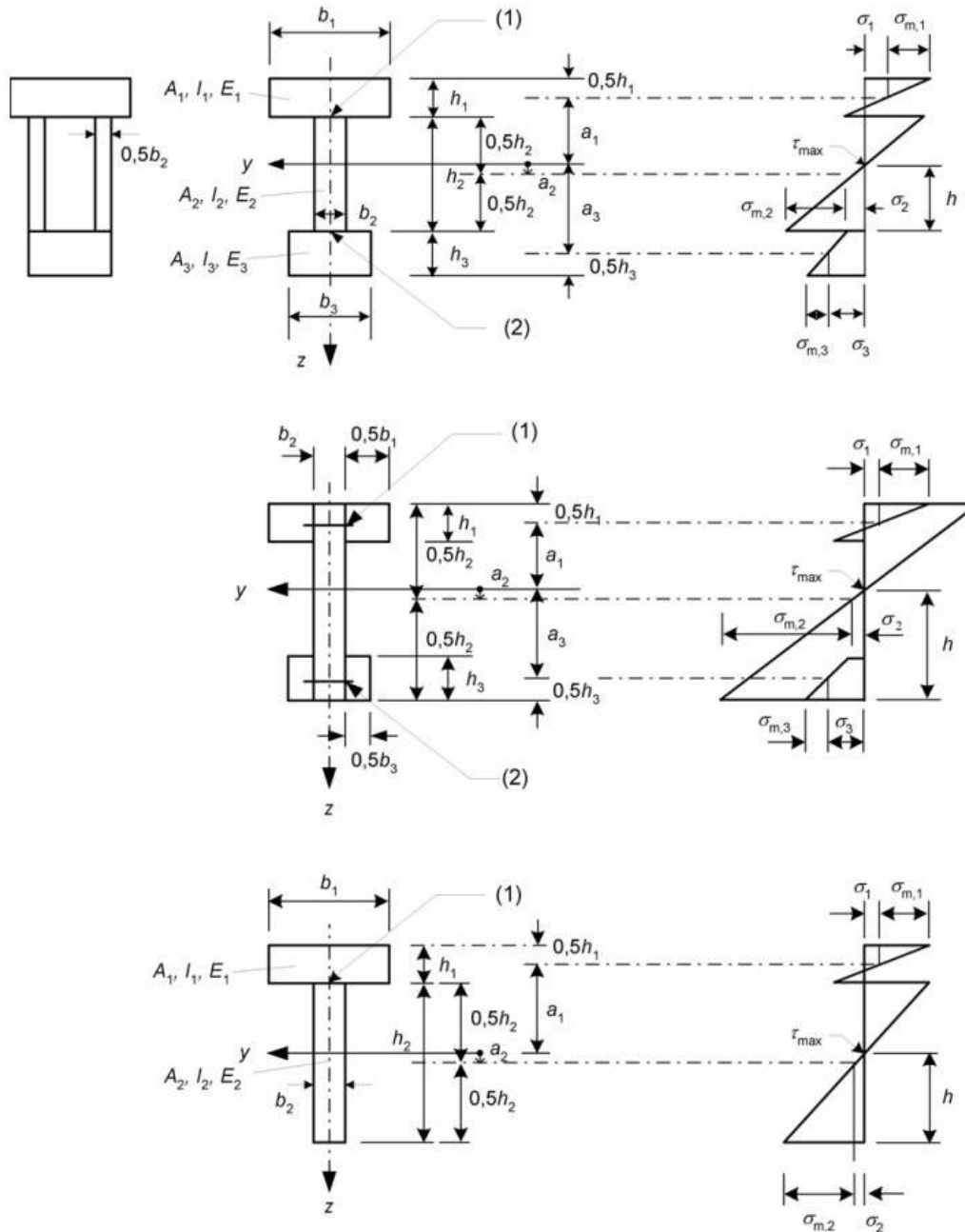
$$R_{c,tip,90,d} = 215 * 340 * 5.6 = 409 \text{ kN} \geq 220 \text{ kN} \checkmark$$

Note: ¹ considering an effective number of screws $n_{eff} = n^{0.9}$ as per [13]
 Required spacing, end and edge distances as per table 6 to be followed

Mechanically jointed beam

Upgrading existing beams can be achieved through several methods. One cost efficient approach is to utilise the mechanically jointed beam theory.

High performance SWG ASSY® VG screws have proven to be a simple and easy to apply tool. Strengthening of an existing timber element is achieved through a mechanical bond of the existing beam and the new lamellas screwed on at the top or bottom of the beam.



Key:

(1) spacing: s₁ slip modulus: K₁ load: F₁
 (2) spacing: s₃ slip modulus: K₃ load: F₃

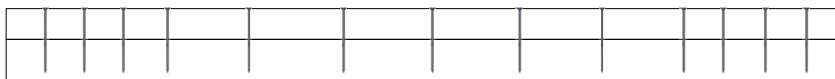
Picture 1: mechanically jointed beams according to [11]

Effective section properties

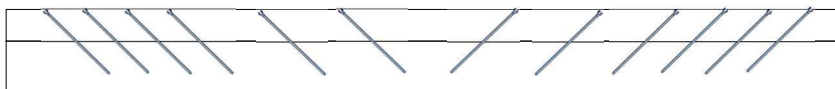
EXAMPLE MECHANICALLY JOINTED BEAM		
<i>Example</i>	GL 24f-E 130 x 456 mm (5-1/8 x 18") single span beam of 5.5 m (18') length with uniform design load of 11.7 kN/m (800 lbf/ft) adding 3 lamellas of 38 mm (1-1/2") of equal grade	
<i>Geometry</i>	$b = 130 \text{ mm} = b_1 = b_2$	beam width
	$h_1 = 3 * 38 = 114 \text{ mm}$	added member depth
	$h_2 = 456 \text{ mm}$	original beam depth
	$A_1 = b * h_1 = 130 * 114 = 14,820 \text{ mm}^2$	cross section of added member
	$A_2 = b * h_2 = 130 * 456 = 59,280 \text{ mm}^2$	cross section of original beam
	$\gamma_m = 1.3$	material safety factor
	$E_{ser} = E_{mean}$	Serviceability modulus of elasticity
	$E_U = E_{mean} / \gamma_m = 12,800 / 1.3 = 9846 \text{ N/mm}^2 = E_1 = E_2$	Ultimate state design modulus of elasticity
	$I_1 = b * h_1^3 / 12 = 16,050,060 \text{ mm}^4$	moment of inertia added member
	$I_2 = b * h_2^3 / 12 = 1,027,203,840 \text{ mm}^4$	moment of inertia original beam
	$s = 152.5 \text{ mm (6")}$	spacing between fasteners
	D	Outer thread diameter
	D_{shank}	Shank diameter
Single span beam: $l_{eff} = l_{span} = 5,500 \text{ mm}$		effective span length [11]
		[multi-span beam: $l_{eff} = 0.8 * l_{span}$
		cantilever : $l_{eff} = 2 * l_{cantilever}$]

Screw arrangements

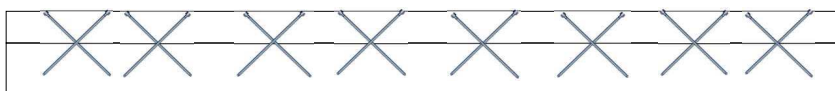
Version 1: *partial thread SWG ASSY® Screws inserted perpendicular*



Version 2: *full thread SWG ASSY® VG Screws inserted at an angle to the grain of $\alpha = 45^\circ$ (one directional)*



Version 3: *full thread SWG ASSY® VG Screws crossed and inserted at an angle to the grain of $\alpha = 45^\circ$*



Shear design with partial thread SWG ASSY® Screws¹

EXAMPLE MECHANICALLY JOINTED BEAM (Version 1)

Bearing reaction	$V = 11.7 * 5.5 / 2 = 32.2 \text{ kN}$
SHEAR DESIGN * WITH PERPENDICULAR PARTIAL THREAD SWG ASSY® SCREWS	
angle between screw axis & wood grain	$\alpha = 90^\circ$
SWG ASSY® screw specifications	SWG ASSY® Ecofast 10 x 240 ($D_{\text{shank}} = 7.2 \text{ mm}$)
boundary conditions for screw design lateral resistance	<p><u>Screw penetration length l_p of SWG ASSY® Ecofast 10 x 240:</u></p> <p>$t_1 = 114 \text{ mm}$ embedment in added member</p> <p>$t_2 = 240 - 114 - 10 = 116 \text{ mm}$ penetration in original beam less one diameter for the tip length</p> <p>$l_p = \min \{t_1; t_2\} = 114 \text{ mm}$</p> <p><u>minimum penetration depth:</u></p> <p>$p_{\min} = 4 * D$ (outside thread diameter) $= 4 * 10 = 40 < 114 \checkmark$ (smaller penetration can not be taken into account for beam reinforcement)</p>
Slip modulus in shear plane [14] ($\rho_k = 0.84 * SG * 10^3$: characteristic gravity)	<p><u>Serviceability:</u> $K_{\text{ser}} = \rho_k^{1.5} / 25 * (D_{\text{shank}})^{0.8} = (0.84 * 0.49 * 10^3)^{1.5} / 25 * 7.2^{0.8} = 1620 \text{ N/mm}$</p> <p><u>Ultimate state:</u> $K_U = 2/3 * K_{\text{ser}} / \gamma_m = 2/3 * 1620 / 1.3 = 831 \text{ N/mm}$</p> <p><u>Ultimate state design:</u> $K_1 = K_U = \mathbf{831 \text{ N/mm}}$ ($K_3 = 0$)</p>
Effectivity of added member eccentricity to inertia [11] ($\gamma_3 = 0$)	<p>$\gamma_1 = 1 / (1 + \pi^2 * E_1 * A_1 * s / (K_1 * I_{\text{eff}}^2))$</p> <p>$= 1 / (1 + \pi^2 * 9,846 * 14,820 * 152.5 / (831 * 5,500^2)) = 0.1027$</p>
Effectivity of original beam eccentricity to inertia [11]	$\gamma_2 = 1$
Distance of single member i centre of gravity to neutral stress axis [11] ($a_3 = 0$)	<p>$a_2 = \gamma_1 * E_1 * A_1 * (h_1 + h_2) / [2 * (\gamma_1 * E_1 * A_1 + 1 * E_2 * A_2 + \gamma_3 * E_3 * A_3)]$</p> <p>$= 0.1027 * 9,846 * 14,820 * (114 + 456) / [2 * (0.1027 * 9,846 * 14,820 + 9,846 * 59,280)]$</p> <p>$= 7.13 \text{ mm}$</p> <p>$a_1 = (h_1 + h_2) / 2 - a_2 = (114 + 456) / 2 - 7.13 = 277.87 \text{ mm}$</p>
Effective moment of inertia [11]	<p>$I_{\text{eff}} = (I_1 + \gamma_1 * A_1 * a_1^2) + (I_2 + 1 * A_2 * a_2^2) + (I_3 + \gamma_3 * A_3 * a_3^2)$</p> <p>$= (16,050,060 + 0.1027 * 14,820 * 277.87^2) + (1,027,203,840 + 1 * 59,280 * 7.13^2)$</p> <p>$= 1,163,784,856 \text{ mm}^4$</p> <p>$(EI)_{\text{eff}} = (E_1 * I_1 + E_1 * \gamma_1 * A_1 * a_1^2) + (E_2 * I_2 + E_2 * 1 * A_2 * a_2^2) + (E_3 * I_3 + E_3 * \gamma_3 * A_3 * a_3^2)$</p> <p>$= E * I_{\text{eff}} = 11,458,625,690,000 \text{ Nmm}^2$</p>
Lateral resistance [1] of one SWG ASSY® VG screw	<p>$P_{r,v} = \text{minimum of shear failure modes } (K_D = K_H = K_{Sf} = K_T = 1)$</p> <p>$= 2.62 \text{ kN (mode g with 114 mm penetration)}$</p>
Lateral design force [11] to be transmitted by one vertical inserted ASSY® screw ¹ ($\alpha = 90^\circ$) → Version 1	<p>$V_{v,1} = V * (E_1 * \gamma_1 * A_1 * a_1 * s) / (EI)_{\text{eff}}$</p> <p>$= 32.2 * (9,846 * 0.1027 * 14,820 * 277.87 * 152.5) / 11,458,625,690,000$</p> <p>$= 1.78 \text{ kN per screw}$</p> <p>$V_{v,3} = V * (E_3 * \gamma_3 * A_3 * a_3 * s) / (EI)_{\text{eff}} = 0$</p>
$P_{r,v} = 2.62 \text{ kN} \geq V_{v,1} = 1.78 \text{ kN} \checkmark$	

Note: ¹ To consider **fastener interaction** the required number of **screws per meter** as per shear design above should be **increased** according to [13] as follows: $n_{\text{req}} = 0.9 \sqrt{n_{\text{perm}}}$

Required spacing, end and edge distances as per *table 6* to be followed

Shear design with full thread SWG ASSY® VG Screws¹

EXAMPLE MECHANICALLY JOINTED BEAM (Version 2 & 3)	
Extern bearing reaction force	$V = 11.7 * 5.5 / 2 = 32.2 \text{ kN}$
SHEAR DESIGN * WITH INCLINED FULL THREAD SWG ASSY® VG SCREWS	
angle between screw axis & wood grain	$\alpha = 45^\circ$
SWG ASSY® screw specifications	SWG ASSY® VG 8 x 330
boundary conditions for screw design withdrawal resistance [12]	<p>penetrated screw length of SWG ASSY® VG Cyl. 8 x 330:</p> $l_{\text{eff},1} = \sqrt{2} * 114 - 15 = 146 \text{ mm}$ thread penetration in added member less un-threaded head $l_{\text{eff},2} = 330 - \sqrt{2} * 114 - 8 = 160 \text{ mm}$ thread penetration in original beam less one diameter for the tip length $l_p = \min \{l_{\text{eff},1}; l_{\text{eff},2}\} = 146 \text{ mm}$ <p>minimum penetration depth: $p_{\text{min}} = 4 * D$ (outside thread diameter) $= 4 * 8 = 32 < 146 \checkmark$ (smaller penetration can not be taken into account for beam reinforcement)</p>
Slip modulus [15,16] (ser: serviceability design U: ultimate design)	<p>Serviceability: $K_{\text{ser}} = 780 * D^{0.2} / (1/l_{\text{eff},1}^{0.4} + 1/l_{\text{eff},2}^{0.4}) = 780 * 8^{0.2} / (1/146^{0.4} + 1/160^{0.4}) = 4419 \text{ N/mm}$ Ultimate state: $K_U = 2/3 * K_{\text{ser}} / \gamma_m = 2266 \text{ N/mm}$ Slip modulus in shear plane (ultimate state design) $K_1 = K_U * \cos^2 \alpha = 1185 * (\cos 45^\circ)^2 = 1133 \text{ N/mm}$</p>
Effectivity of added member eccentricity to inertia [11] ($\gamma_3 = 0$)	$\gamma_1 = 1 / (1 + \pi^2 * E_1 * A_1 * s / (K_1 * l_{\text{eff}}^2))$ $= 1 / (1 + \pi^2 * 9,846 * 14,820 * 152.5 / (1133 * 5,500^2)) = 0.1350$
Effectivity of original beam eccentricity to inertia [11]	$\gamma_2 = 1$
Distance of single member i centre of gravity to neutral stress axis [11] ($a_3 = 0$)	$a_2 = [\gamma_1 * E_1 * A_1 * (h_1 + h_2) / (2 * (\gamma_1 * E_1 * A_1 + 1 * E_2 * A_2 + \gamma_3 * E_3 * A_3))]$ $= [0.1350 * 9,846 * 14,820 * (114 + 456)] / [2 * (0.1350 * 9,846 * 14,820 + 9,846 * 59,280)]$ $= 9.30 \text{ mm}$ $a_1 = (h_1 + h_2) / 2 - a_2 = (114 + 456) / 2 - 9.30 = 275.7 \text{ mm}$
Effective moment of inertia [11]	$I_{\text{eff}} = (I_1 + \gamma_1 * A_1 * a_1^2) + (I_2 + 1 * A_2 * a_2^2) + (I_3 + \gamma_3 * A_3 * a_3^2)$ $= (16,050,060 + 0.1350 * 14,820 * 275.7^2) + (1,027,203,840 + 1 * 59,280 * 9.30^2)$ $= 1,200,455,215 \text{ mm}^4$ $(EI)_{\text{eff}} = (E_1 * I_1 + E_1 * \gamma_1 * A_1 * a_1^2) + (E_2 * I_2 + E_2 * 1 * A_2 * a_2^2) + 0$ $= E * I_{\text{eff}} = 11,819,682,040,000 \text{ Nmm}^2$
Withdrawal resistance of one SWG ASSY® VG screw (refer to table 1)	<p>withdrawal resistance [1.37 kN/20 mm] * 146 = 10 kN tensile resistance: 19.2 kN</p>
Tensile design force $V_{t,i}$ [11] to be transmitted by one inclined reinforcing ASSY® VG screw ¹ ($\alpha = 45^\circ$) → Version 2 ($V_{v,3} = V_{t,3} = 0$)	$V_{v,1} = V * (E_1 * \gamma_1 * A_1 * a_1 * s) / (EI)_{\text{eff}}$ $= 32.2 * (9,846 * 0.1350 * 14,820 * 275.7 * 152.5) / 11,819,682,040,000$ $= 2.26 \text{ kN per screw}$ $V_{t,1} = V_{v,1} / (\cos \alpha) = 1.78 / \cos 45^\circ = 3.19 \text{ kN per screw}$
$P_{r,v} = 10 \text{ kN} \geq V_{v,1} = 3.19 \text{ kN} \checkmark$	
Tensile design force $V_{t,i}$ [11] to be transmitted by one crossed reinforcing ASSY® VG screw ¹ → Version 3	$V_{t,1} = V_{v,1} / (2 * \cos \alpha) = 2.26 / (2 * \cos 45^\circ) = 1.60 \text{ kN per screw}$
$P_{r,v} = 10 \text{ kN} \geq V_{v,1} = 1.60 \text{ kN} \checkmark$	

Note: ¹ To consider **fastener interaction** the required number of **screws per meter** as per shear design above should be **increased** according to [13] as follows: $n_{\text{req}} = 0.9 \sqrt{n_{\text{per m}}}$. Required spacing, end and edge distances as per **table 6** to be followed

Design tables for SWG ASSY® VG screws

Table 1: Factored withdrawal resistance of SWG ASSY® VG screws in kN per 20 mm of thread penetration

Factored withdrawal resistance * P' _{rw,α} per 20 mm of thread penetration in kN (only applicable to SWG ASSY® VG screws)							
Screw diameter in mm	Mean oven dry relative density						Factored tensile resistance in kN
	0.35	0.42	0.44	0.46	0.49	0.50 (PSL)	
	α ** = 90°						
6	0.63	0.91	0.97	1.06	1.20	0.70	9.04
8	0.85	1.22	1.29	1.41	1.60	0.94	15.12
10	1.06	1.52	1.61	1.76	2.00	1.17	19.2
12	1.27	1.83	1.94	2.12	2.40	1.41	24
	α ** = 45°						
6	0.54	0.78	0.83	0.91	1.03	0.60	9.04
8	0.73	1.04	1.11	1.21	1.37	0.80	15.12
10	0.91	1.31	1.38	1.51	1.71	1.00	19.2
12	1.09	1.57	1.66	1.81	2.06	1.21	24

Note: * resistance as per [12]

** α : angle between wood grain and screw axis

Table 2: values of k_α for standard beam sizes and connections

Values for k_α with respect to the ratio h_e/h										
h_e/h	0_0	0_1	0_2	0_3	0_4	0_5	0_6	0_7	0_8	0_9
0.5_	0.650	0.631	0.611	0.592	0.572	0.553	0.534	0.514	0.495	0.476
0.6_	0.458	0.439	0.420	0.402	0.384	0.366	0.349	0.331	0.314	0.297
0.7_	0.281	0.265	0.249	0.233	0.218	0.203	0.189	0.175	0.161	0.148
0.8_	0.135	0.123	0.111	0.100	0.089	0.079	0.069	0.060	0.052	0.044
0.9_	0.036	0.030	0.024	0.018	0.013	0.009	0.006	0.003	0.002	0.000

Table 3: values of k_{tp} for standard beam sizes and connections

Values for k_{tp} with respect to the ratio a/h										
a/h	0_0	0_1	0_2	0_3	0_4	0_5	0_6	0_7	0_8	0_9
0.5_	0.500	0.485	0.470	0.455	0.440	0.425	0.410	0.396	0.381	0.366
0.6_	0.352	0.338	0.323	0.309	0.295	0.282	0.268	0.255	0.242	0.229
0.7_	0.216	0.204	0.191	0.179	0.168	0.156	0.145	0.134	0.124	0.114
0.8_	0.104	0.095	0.086	0.077	0.069	0.061	0.053	0.046	0.040	0.034
0.9_	0.028	0.023	0.018	0.014	0.010	0.007	0.005	0.003	0.001	0.000

Design assumptions for SWG ASSY® VG screws as reinforcement

Table 4: buckling resistance * of one screw considering an angle between screw axis to wood grain of $\alpha = 90^\circ$

buckling resistance* $\kappa_c \cdot N_{pl,d}$ in [kN (lbf)] of one SWG ASSY® VG screw								
specific gravity SG	Outer thread diameter							
	mm , kN	inch, lbf	mm , kN	inch, lbf	mm , kN	inch, lbf	mm , kN	inch, lbf
	6	1/4	8	5/16	10	3/8	12	1/2
0.42	6.10	1370	11.05	2481	16.56	3720	24.64	5535
0.49	6.30	1416	11.42	2566	17.07	3835	25.51	5731
0.5	6.33	1422	11.47	2577	17.13	3849	25.62	5756

Note: * resistance according to [17] considering an angle between screw axis and wood grain direction of $\alpha = 90^\circ$

Table 5: timber densities

Timber densities		
Visually graded lumber	Glue-laminated timber	Mean oven dry relative density
Northern Species		0.35
Spruce-Pine-Fir		0.42
	Spruce-Pine-Fir	0.44
Hem-Fir	Hem-Fir	0.46
Douglas-Fir-Larch D-Fir-L	Douglas-Fir-Larch D-Fir-L	0.49
PSL, LVL, LSL	PSL, LVL, LSL	0.5

Table 6: Minimum spacing or distance for SWG ASSY® VG screws

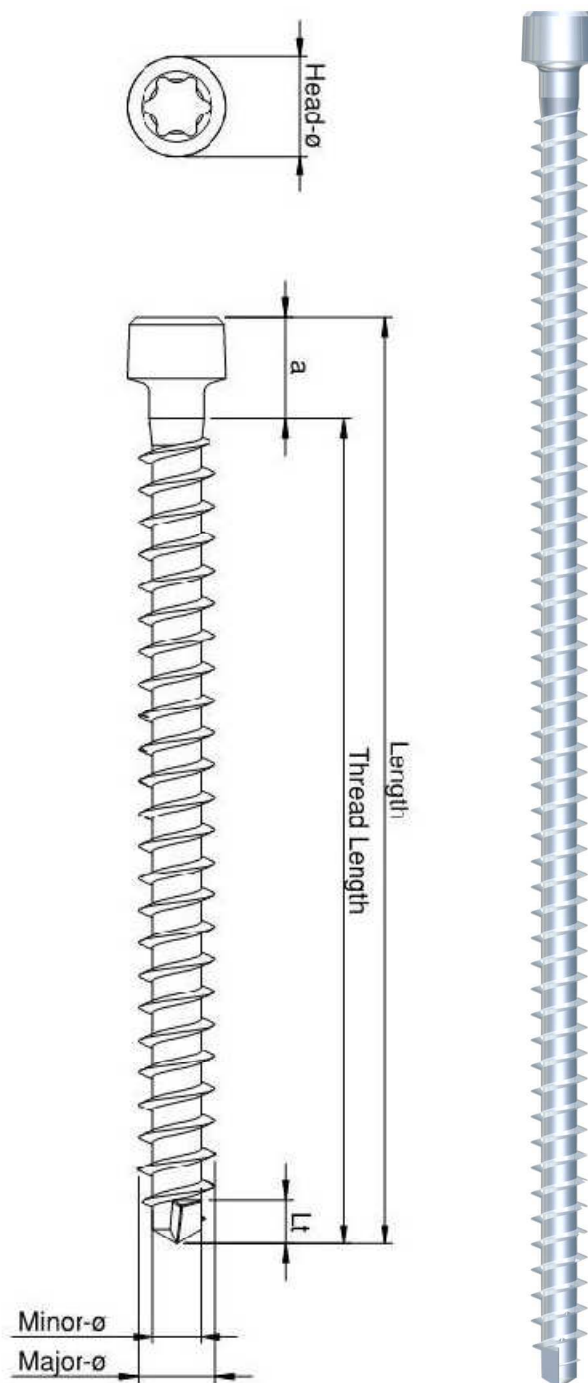
SWG ASSY® VG screws loaded axially	
Minimum spacing or distance [12]	(D = outside thread diameter)
S_p Spacing parallel to grain	5D (7.5D in D-Fir-L)
S_Q Spacing perpendicular to grain	2.5D
a_L end distance	5D (7.5D in D-Fir-L)
e_L edge distance	3D

SWG ASSY® VG Cyl. (full thread)

Table 7: SWG ASSY® VG Cyl screw specifications

Major Ø	Length	Thread Length	L _t	Head Ø	Minor Ø	Bit
mm						
6	70	63	6	8	3.8	AW 30
	80	73				
	100	93				
	120	113				
	140	133				
	160	153				
	180	173				
	200	193				
8	160 to 300 in 20 mm increments	144 to 284 in 20 mm increments	8	10	5	AW 40
	330	314				
	360	344				
	380	364				
	430	414				
	480	464				
	530	514				
	580	564				
10	140 to 280 in 20 mm increments	125 to 265 in 20 mm increments	10	13.4	6.2	AW 50
	300	280				
	320 to 400 in 20 mm increments	305 to 380 in 20 mm increments				
	430	415				
	480	456				
	530	506				
	580	556				
	and longer	and longer				

Note: values listed in the table above are average measurements between upper and lower tolerance boundary

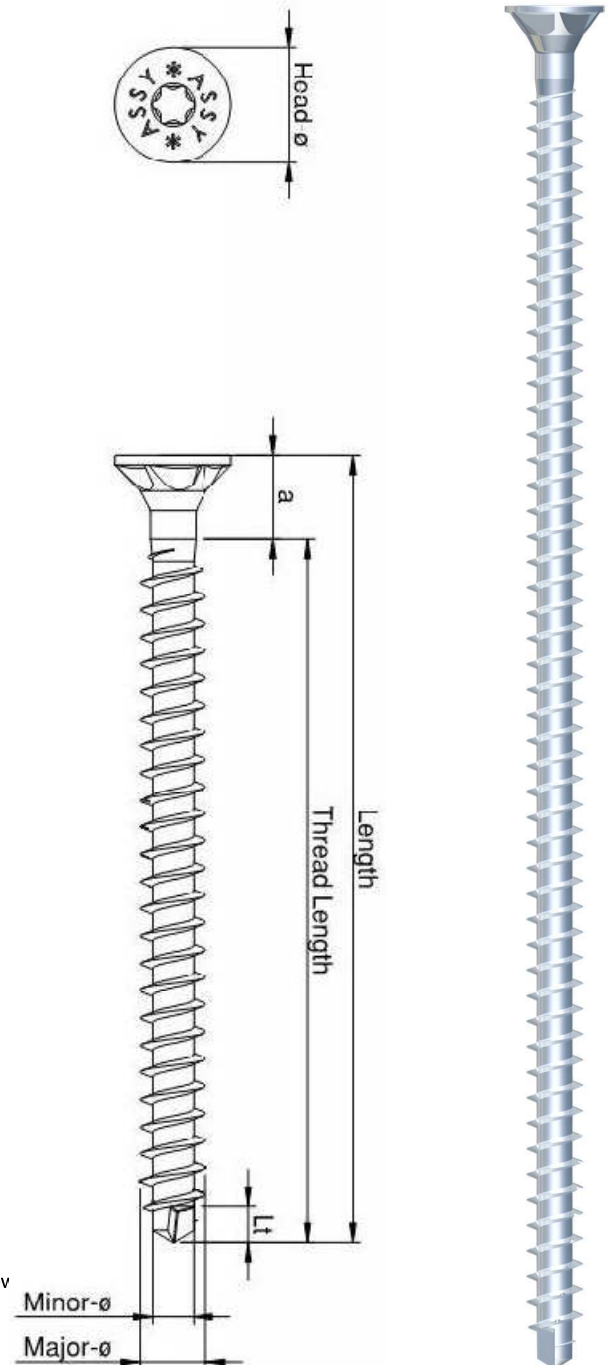


SWG ASSY® VG CSK (full thread)

Table 8: SWG ASSY® VG CSK screw specifications

Major Ø	Length	Thread Length	L _t	Head Ø	Minor Ø	Bit
mm						
8	120	103	8	14.8	5	AW 40
	140	123				
	160	143				
	180	163				
	200	183				
	220	203				
	240	223				
	260	243				
	280	263				
	300	283				
10	140 to 400 in 20 mm increments	125 to 385 in 20 mm increments	10	19.6	6.2	AW 50
	430	415				
	480	465				
	530	512				
	580	562				
12	650 to 800 in 50 mm increments	632 to 782 in 50 mm increments	12	22.1	7.1	AW 50
	220	205				
	380	365				
	480	465				
	600	585				

Note: values listed in the table above are average measurements between upper and low tolerance boundary



References

- [1] CSA 086-09
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- [3] European Technical Approval ETA-11/0190: A.3.2.1 *Connection forces at an angle to the grain*
- [4] Eurocode 5—DIN EN 1995-1-1/NA:2010-12: NA.6.8.4
- [5] Eurocode 5—DIN EN 1995-1-1/NA:2010-12: NA.6.7 (NA.4)
- [6] Eurocode 5—DIN EN 1995-1-1:2010-12: 6.4.3 (7) & (8) *Double tapered, curved and pitched cambered beams*
- [7] Eurocode 5—DIN EN 1995-1-1/NA:2010-12: NA.6.8.6
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- [9] Eurocode 5—DIN EN 1995-1-1:2010-12: 6.1.5(1)
- [10] European Technical Approval ETA-11/0190: Annex 2 *Compression reinforcement perpendicular to the grain*
- [11] Eurocode 5—DIN EN 1995-1-1:2010-12: B.2 *Effective bending stiffness*
- [12] CCMC report 'CCMC 13677-R'
- [13] Eurocode 5—DIN EN 1995-1-1:2010-12: 8.7.2(8) *Axially loaded screws*
- [14] DIN 1052-2004: G.1 *Slip modulus for slender fasteners*
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- [16] Francois Colling, *Holzbau: Grundlagen und Bemessung nach EC5*, Springer Vieweg, Mering (Germany), 2012 3. edition, p.290/291
- [17] European Technical Approval ETA-11/0190: A.1.3.3 *Compressive capacity*

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info@my-ti-con.com

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